

## Fractions

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- Adding and Subtracting
  - Need common denominator
  - Add or subtract on top, keep denominator
- Multiplication
  - Improper fractions first
  - Multiply top AND bottom
    - Simplify and multiply or multiply and simplify
- Division
  - Keep, change, flip – K.C.F.
  - Then multiply

## Operations with Postive and Negative Numbers

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- Adding and Subtracting
  - Negative plus negative – REALLY negative!
  - Different signs – sign of answer determined by “larger” number
  - Adding a negative is the same as subtracting
    - Ex.  $6 + (-8) = 6 - 8$
  - Minus a negative is plus
    - Ex.  $3 - (-4) = 3 + 4$
- Multiplication and Division
  - Same signs – answer is positive
  - Different signs – answer is negative
  - Bigger or smaller doesn't matter

## Order of Operations and Exponents

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- Order of Operations
  - PEMDAS
  - Multiply/Divide and Add/Subtract L->R
- Exponents
  - What is being taken to the exponent?
    - $-4^3 \neq (-4)^3$
  - Pull it apart to simplify if you're not sure.
    - Multiplying – add exponents
    - Dividing – subtract exponents
    - Power to a power – multiply exponents

## FOIL, Distributive Property, Like Terms

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- FOIL – first, outer, inner, last
  - Multiplying two binomials
  - Ex.  $(x - 4)(x + 3)$
- Distributive Property
  - Multiply number outside parenthesis by EVERY term inside
  - Minus signs go with number that follows
  - Ex.  $4(x - 7) = 4(x + (-7))$
- Like Terms
  - Must have the same variable(s) to the same exponent
  - Ex.  $4x, -7x$     $3, 9$     $5xy^2, -11xy^2$

## Writing and Solving Inequalities

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- Read the Symbols
  - $<, \leq, \geq, >$
  - “L” less than
- Writing Inequalities
  - Not sure, pick something you know works and write inequality
  - Careful: “at least”, “no more than”, “no less than”, etc.
  - No fighting inequalities!  $< x >$  can never be true!
- Solving
  - Just like equations, except...
    - When multiplying or dividing by a negative on BOTH sides
    - Write final answer with variable first. Ex.  $4 < x$  is  $x > 4$ .
- Graphing on Number Line
  - $< >$ , open circle    $| | \leq \geq$ , filled in circle
  - Numbers under line should work
  - Follow the inequality symbol IF the variable is written first.

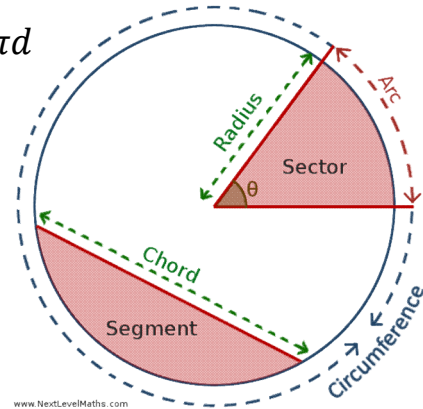
## Solving Absolute Value Equations

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- A Number’s Distance From Zero
  - Always positive
- Solving
  - Isolate the absolute value
  - Write two equations
    - 1. Easy one – forget the absolute value
    - 2. Second one – take the opposite
  - Solve
  - Check by plugging back in
    - Watch for negatives: Ex.  $|x - 3| = -2$  Not possible!

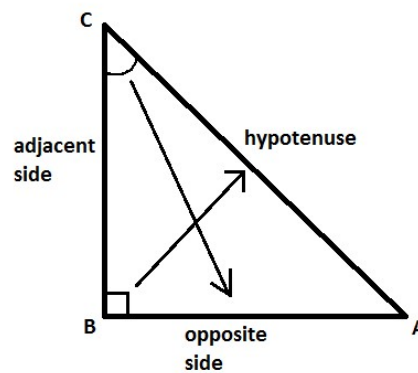
## Circles

- Vocabulary
- Perimeter... circumference  $\rightarrow 2\pi r$  or  $\pi d$
- Area... square units  $\rightarrow \pi r^2$
- 360 degrees



## SOHCAHTOA

- Right triangles
- Can be used to find missing sides and/or angles



$$\sin c = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{AB}{AC}$$

$$\cos c = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{BC}{AC}$$

$$\tan c = \frac{\text{opposite}}{\text{adjacent}} = \frac{AB}{BC}$$

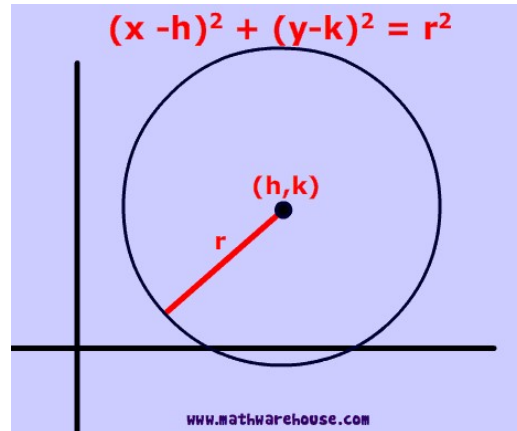
$$\cot c = \frac{\text{adjacent}}{\text{opposite}} = \frac{BC}{AB}$$

$$\sec c = \frac{\text{hypotenuse}}{\text{adjacent}} = \frac{AC}{BC}$$

$$\csc c = \frac{\text{hypotenuse}}{\text{opposite}} = \frac{AC}{AB}$$

## Circle Equation

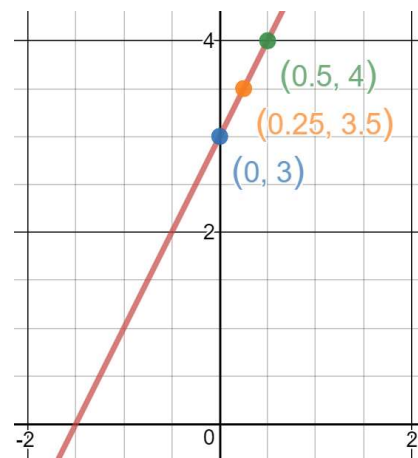
- Graphing circles on coordinate plane.
- Need center and radius.
- Careful with negatives...  
Ex.  $(x - 3)^2 + (y + 2)^2 = 25$   
center: (3, -2), radius: 5



## Graphing on Coordinate Plane

$$y = 2x + 3$$

- A picture is worth a 1,000 words!
- All possible ordered pairs that are solutions  $(x, y)$  to the equation.
- Shortcuts
  - $y = mx + b$
  - Can ALWAYS plug in values to get ordered pairs.
- Technology



## Formulas

- When do we use these?

$SA = ph + 2B$ $SA = \pi r l + \pi r^2$ $SA = 4\pi r^2$	$SA$ = surface area $B$ = area of base $h$ = height $p$ = perimeter $r$ = radius $l$ = slant height
$V = Bh$ $V = \frac{1}{3}Bh$ $V = \frac{4}{3}\pi r^3$	$V$ = volume $B$ = area of base $h$ = height $r$ = radius

Pythagorean Theorem	$a^2 + b^2 = c^2$
Distance formula	$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
Quadratic formula	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
Trigonometric Relations	$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$ $\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$ $\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$
$A = \pi r^2$ $C = \pi d$	$A$ = area $C$ = circumference $d$ = diameter $r$ = radius

## Domain, Range and Excluded Values

- Domain: x-values (what we can put into the equation)
  - Watch out for things we can't do
    - Examples: divide by zero, take square root of a negative
- Range: y-values (what we get out of an equation)
  - What numbers are possible to get out?
    - Examples: can't get a negative out of an absolute value
- Excluded Values
  - Values that get us into "trouble"
- Hint: Graph it!

## Word Problems

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- What is the problem asking for?
- What do we know?
- Strategies
  - Draw a picture
  - Look at a similar problem
  - Pick some “easy” numbers to work with
  - Read the problem several times
- Does answer make sense?
- Did we answer the whole question?

## Logarithms

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- Answer to a logarithm is an exponent.
- Inverse of exponential

<b>Logarithm = Exponent</b>
$\log_a N = x \iff N = a^x$
(Common Log) $\log N = x \iff N = 10^x$
(Natural Log) $\ln N = x \iff N = e^x$